

Chemistry , Class 11th , 21/08/2020 , Gaseous State

Test :- 6-7
(Saturday)

Liquefaction of Gases :-

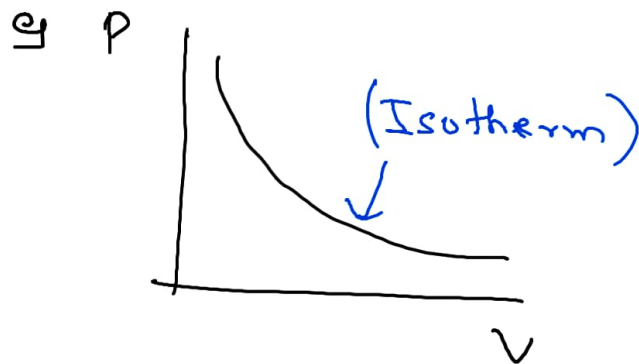
* Gases can be liquefied by decrease in temp. & increase in pressure.

★

Isothermal \rightarrow Temp. constant

Isobaric \rightarrow Pressure constant

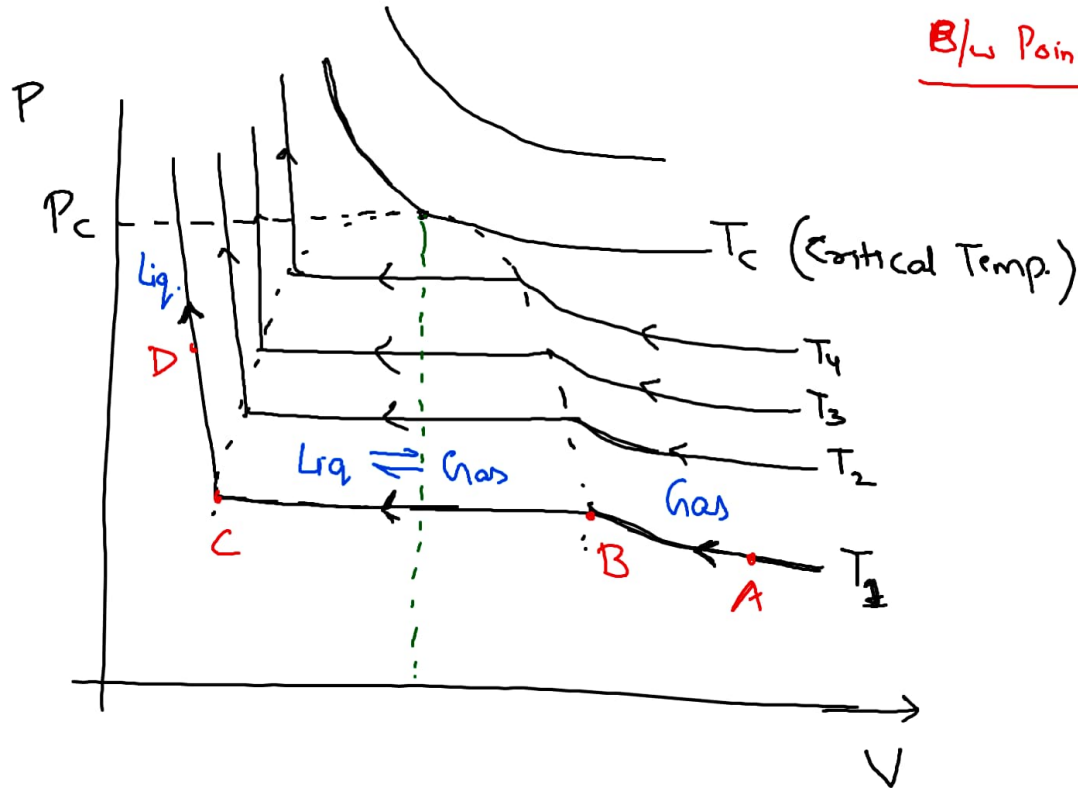
Isochoric \rightarrow Volume constant



(Ideal gas)

(At constant temp.)

Andrew's Isotherm :-



Point A :- Gas Phase

B/w Point A & B :- Real gas compression occurs.

Point B :- Liquefaction of gas starts

B/w Point B & C :- Liq. & Gas are in equilibrium

Point C :- Almost gas is liquefied

Point D :- Negligible compression of liquid

Critical Temp. (T_c) :-

The temp. above which a gas cannot be liquified is called as T_c

Critical Pressure (P_c) :-

The pressure required to liquify a gas at critical temp. is called as Critical Pressure.

Critical Volume (V_c) :-

The vol. of 1 mole of gas at T_c & P_c is called as Critical Volume.

For 1 mole of gas :-

$$\left(P + \frac{a}{V^2}\right)(V-b) = RT$$

$$PV + \frac{a}{V} - Pb - \frac{ab}{V^2} = RT$$

$$PV^3 + aV - PbV^2 - ab = V^2RT$$

Divide by P

$$V^3 + \frac{a}{P}V - bV^2 - \frac{ab}{P} = \frac{V^2RT}{P}$$

① -
$$V^3 - V^2\left(b + \frac{RT}{P}\right) + \frac{a}{P}V - \frac{ab}{P} = 0$$

$$(V-v_1)(V-v_2)(V-v_3) = 0$$

At critical point

$$V_1 = V_2 = V_3 = V_c$$

$$(V-V_c)^3 = 0$$

$$V^3 - V_c^3 - 3VV_c(V-V_c) = 0$$

$$V^3 - V_c^3 - 3V_cV^2 + 3V_c^2V = 0$$

②
$$V^3 - 3V_cV^2 + 3V_c^2V - V_c^3 = 0$$

From eqn ① at critical conditions

$$V^3 - V^2 \left(b + \frac{RT_c}{P_c} \right) + \frac{a}{P_c} V - \frac{ab}{P_c} = 0 \quad \text{--- ③}$$

$$V^3 - 3V_c V^2 + 3V_c^2 V - V_c^3 = 0 \quad \text{--- ②}$$

Comparing coefficients of eqn ② & ③

$$b + \frac{RT_c}{P_c} = 3V_c \quad \text{④}$$

$$\frac{a}{P_c} = 3V_c^2 \quad \text{⑤}$$

$$\frac{ab}{P_c} = V_c^3 \quad \text{⑥}$$

$$b + \frac{RT_c}{P_c} = 3V_c$$

↳ (4)

$$\frac{a}{P_c} = 3V_c^2$$

↳ (5)

$$\frac{ab}{P_c} = V_c^3$$

↳ (6)

(6) / (5)

$$\frac{\cancel{ab}}{\cancel{P_c}} \times \frac{\cancel{P_c}}{a} = \frac{V_c^3}{3V_c^2}$$

$$V_c = 3b$$

Substitute value of V_c
in eqn (5)

$$\frac{a}{P_c} = 3(3b)^2$$

$$P_c = \frac{a}{27b^2}$$

Substitute value of P_c & V_c in (4)

$$b + \frac{RT_c}{P_c} = 3 \times 3b$$

$$\frac{RT_c}{P_c} = 8b$$

$$T_c = 8b \times \frac{a}{27b^2} \times \frac{1}{R}$$

$$T_c = \frac{8a}{27Rb}$$

~~1/2~~

Gas having higher value of T_c
can be liquefied easily.

~~1/2~~

$$T_c = \frac{8a}{27Rb}$$

$a \Rightarrow$ attraction forces

$a \uparrow$, $T_c \uparrow$, Easily liquefied.

Compressibility factor at Critical Conditions :-

$$Z = \frac{P_c V_c}{RT_c}$$

$$Z = \frac{a}{27b^2} \times \frac{3b}{R \times \frac{8a}{27Rb}}$$

$$Z = \frac{a}{27b^2} \times \frac{3b}{8a} \times 27b$$

~~1/2~~

$$Z = \frac{3}{8}$$